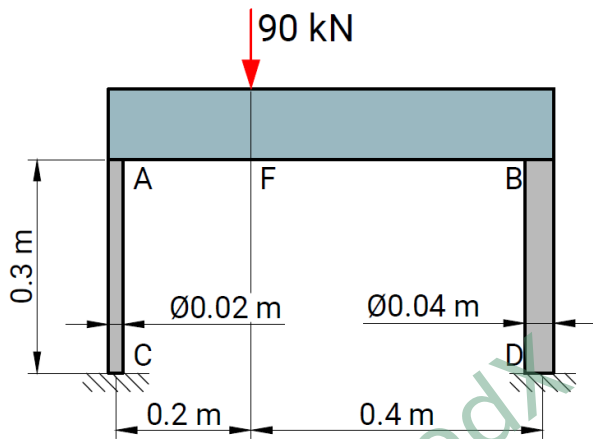


Problem 2

Figure



Description

A rigid horizontal beam AB is supported by two vertical posts as shown.

Post AC is made of steel with a diameter of 20 mm, and post BD is made of aluminum with a diameter of 40 mm. The beam is rigid, and a vertical load of 90 kN is applied at point F, located 200 mm from A and 400 mm from B. The height of each post is 300 mm.

Given the material properties

$$E_{st} = 2.0 \times 10^8 \text{ kN/m}^2$$

$$E_{al} = 7.0 \times 10^7 \text{ kN/m}^2$$

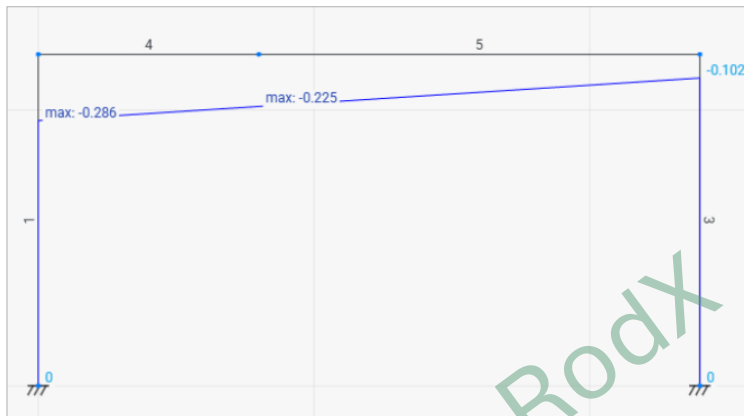
Determine:

- Vertical displacement of point F on the rigid beam

Model

Units:	m, kN
Element:	Beam element
Material:	Steel, $E = 2.0 \times 10^8 \text{ kN/m}^2$; Aluminum, $E = 7.0 \times 10^7 \text{ kN/m}^2$
Section property:	D (steel bar) = 0.02 m; D (aluminum bar) = 0.04 m
Constraints:	Fixed at point C, D
Load Case:	Beam concentrated load -90 kN are applied at nodes F in the Y direction.

Results



Project Title:		Untitled Project		
Load Case/Combination:		LC0 - Default Case		
Units:		mm		
Element	x/L	Ux	Uy	Ur
1	0	0	0	0
1	1	-0.0461	-0.2864	0.000306
3	0	-0.0461	-0.10237	0.000308
3	1	0	0	0
4	0	-0.0461	-0.2864	0.000306
4	1	-0.0461	-0.22525	0.000306
5	0	-0.0461	-0.22525	0.000306
5	1	-0.0461	-0.10237	0.000308

Comparison of Results

Node	Deformation, mm		
	Theoretical	RodX	Midas/Civil
$\Delta x(A)$	-0.286	-0.286	-0.286
$\Delta x(F)$	-0.225	-0.225	-0.225
$\Delta x(D)$	-0.102	-0.102	-0.102

Reference

- Hibbeler R. C, Mechanics of Materials, 10th Edition in SI units, 2017, Pearson, example 4.3, p.149